

Advanced Algebra
6.4 Worksheet

Name Answers
Period _____

Solve Each Equation. Give exact answers and state any multiplicity.

1. $x^4 - 5x^2 + 4 = 0$

2. $x^4 - 23x^2 = 50$

1. $x = \pm 2$ and ± 1

$$(x^2 - 4)(x^2 - 1) = 0$$

$$\begin{array}{r} x^2 - 4 = 0 \\ +4 \quad +4 \\ \hline x^2 = 4 \end{array}$$

$$\begin{array}{r} x^2 - 1 = 0 \\ +1 \quad +1 \\ \hline x^2 = 1 \end{array}$$

$$\sqrt{x^2} = \sqrt{4}$$

$$\sqrt{x^2} = \sqrt{1}$$

2. _____

3. $-14 = x^4 - 9x^2$

4. $x^4 + 13x^2 = -36$

3. _____

4. _____

5. $x^4 - 12x^2 + 11 = 0$

6. $x^4 - 8x^2 + 16 = 0$

5. _____

6. _____

7. $x^4 - 36 = 0$

8. $9x^4 = 49$

7. _____

$$9x^4 - 49 = 0$$

$$(3x^2 - 7)(3x^2 + 7) = 0$$

8. $\pm \sqrt{7/3}$ and $\pm i\sqrt{7/3}$

$$\begin{array}{r} 3x^2 - 7 = 0 \\ +7 \quad +7 \\ \hline 3x^2 = 7 \end{array}$$

$$\begin{array}{r} 3x^2 + 7 = 0 \\ -7 \quad -7 \\ \hline 3x^2 = -7 \end{array}$$

$$\frac{3x^2}{3} = \frac{7}{3}$$

$$\frac{3x^2}{3} = \frac{-7}{3}$$

$$x^2 = 7/3$$

$$x^2 = -7/3$$

$$x = \pm \sqrt{7/3}$$

$$x = \pm i\sqrt{7/3}$$

9. $x^3 = 64$

10. $8x^4 + x = 0$

9. _____

$$x(8x^3 + 1) = 0$$

$$x(2x+1)(4x^2 - 2x + 1) = 0$$

10. $x = 0, -\frac{1}{2}, \text{ and } \frac{1 \pm i\sqrt{3}}{4}$

$x = 0$

$$2x+1=0$$

$$\frac{2x}{2} = \frac{-1}{1}$$

$$\frac{2 \pm \sqrt{(-2)^2 - 4(4)(1)}}{2(4)}$$

11. $x^3 + 27 = 0$

12. $125 = 8x^3$

$$\frac{2 \pm \sqrt{-12}}{8}$$

11. _____

$$\frac{2 \pm 2i\sqrt{3}}{8}$$

12. _____

$$\frac{1 \pm i\sqrt{3}}{4}$$