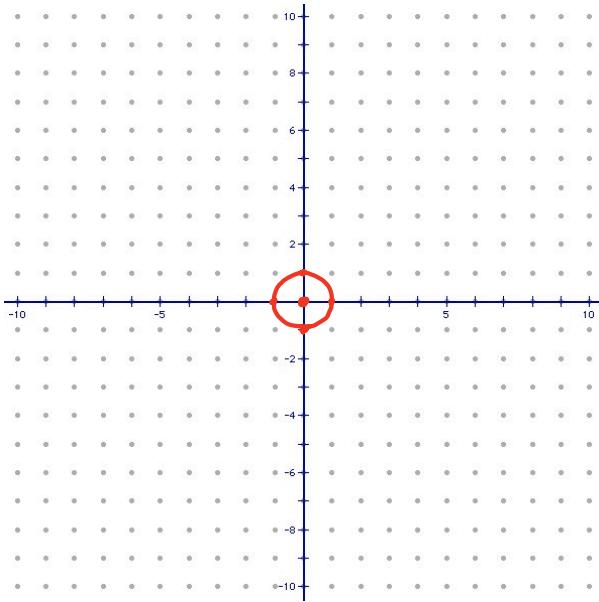


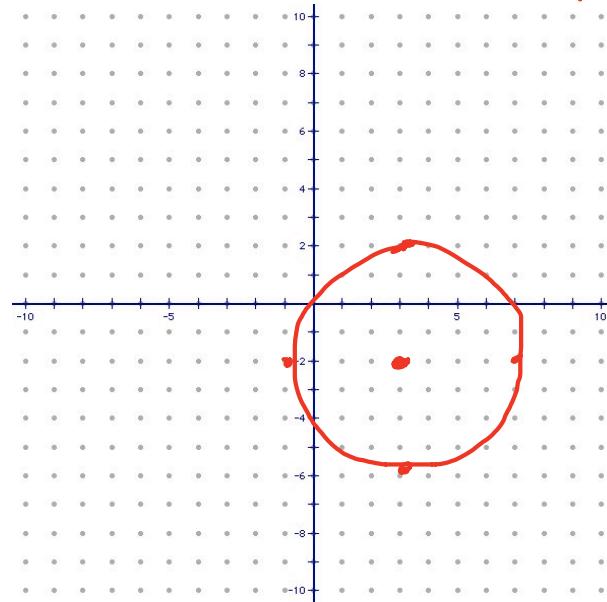
## Review...Graphing Circles

Standard Form of a Circle:  $(x-h)^2 + (y-k)^2 = r^2$ , where  $(h, k)$  = center and  $r$  = radius.

Graph  $x^2 + y^2 = 1$ . Center:  $(0, 0)$   
r : 1



Graph  $(x-3)^2 + (y+2)^2 = 16$ . Center:  $(3, -2)$   
r = 4



$$(x-h)^2 + (y-k)^2 = r^2$$

## Review...Completing the Square

Ex. Complete the square to change to standard form of a circle.

a)  $x^2 + y^2 - 4x + 10y + 20 = 0$

$$\begin{aligned} & \cancel{(x^2 - 4x + 4)}_{(x-2)^2} + \cancel{(y^2 + 10y + 25)}_{(y+5)^2} + 20 - \cancel{4} - \cancel{25} = 0 \\ & (x-2)^2 + (y+5)^2 - 9 = 0 \\ & \boxed{(x-2)^2 + (y+5)^2 = 9} \end{aligned}$$

b)  $4x^2 + 4y^2 - 16x - 24y + 51 = 0$

$$\begin{aligned} & 4x^2 - 16x + 4y^2 - 24y \\ & 4\cancel{(x^2 - 4x + 4)}_{(x-2)^2} + 4\cancel{(y^2 - 6y + 9)}_{(y-3)^2} + 51 - \cancel{16} - \cancel{36} = 0 \\ & 4(x-2)^2 + 4(y-3)^2 = 1 \quad \boxed{(x-2)^2 + (y-3)^2 = \frac{1}{4}} \end{aligned}$$