

What is the Quadratic Formula?

It gives the solutions of the equation $ax^2 + bx + c = 0$.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Use parentheses when substituting

$(b)^2$ will always be a positive value.

$$6x^2 - x - 15 = 0$$

$a = 6$ $b = -1$ $c = -15$

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(6)(-15)}}{2(6)}$$

$$\frac{1 \pm \sqrt{1 + 361}}{12}$$

$$\frac{1 \pm \sqrt{361}}{12} \begin{cases} + \rightarrow \frac{1 + \sqrt{361}}{12} = \frac{1 + 19}{12} = \frac{20}{12} \\ - \rightarrow \frac{1 - \sqrt{361}}{12} = \frac{1 - 19}{12} = \frac{-18}{12} \end{cases}$$

$x = \frac{20}{12} = \frac{5}{3}$ $x = \frac{-18}{12} = \frac{-3}{2}$
 $x = 1.\bar{6}$ $x = -1.5$

$$2x^2 + 7x + 15 = 0$$

$a = 2$ $b = 7$ $c = 15$

$$x = \frac{-(7) \pm \sqrt{(7)^2 - 4(2)(15)}}{2(2)}$$

$$\frac{-7 \pm \sqrt{49 - 120}}{4}$$

$$\frac{-7 \pm \sqrt{-71}}{4}$$

No Real Solution

$$3x^2 - 16x = 0$$

$a = 3$ $b = -16$ $c = 0$

$$x = \frac{-(-16) \pm \sqrt{(-16)^2 - 4(3)(0)}}{2(3)}$$

$$\frac{16 \pm \sqrt{256 - 0}}{6}$$

$$\frac{16 + \sqrt{256}}{6} \quad \frac{16 - \sqrt{256}}{6}$$

$$\frac{16 + 16}{6} \quad \frac{16 - 16}{6}$$

$x = \frac{32}{6} = \frac{16}{3}$ $x = \frac{0}{6} = 0$
 $x = 5.\bar{3}$