

Cumulative 3-4 Review

Name KEY

1) Solve each equation.

a) $7 - \frac{w}{2} = 9$

$$\begin{array}{r} \cancel{7} - \frac{w}{2} = 9 \\ \cancel{-7} \quad \quad \quad \cancel{-7} \end{array}$$

$$\cancel{(-2)} \cdot \frac{-w}{2} = 2 \cdot (-2)$$

$$\boxed{w = -4}$$

c) $3x + 7 = 5x - 13$

$$\begin{array}{r} \cancel{3x} + 7 = 5x - 13 \\ \cancel{-3x} \quad \quad \quad \cancel{-3x} \end{array}$$

$$\begin{array}{r} 7 = 2x - 13 \\ +13 \quad \quad \quad +13 \end{array}$$

$$\frac{20}{2} = \frac{2x}{2}$$

$$\boxed{10 = x}$$

e) $7.4 + (-5.1x) + 3.2x = 20.8$

$$\begin{array}{r} \cancel{7.4} + -1.9x = 20.8 \\ \cancel{-7.4} \quad \quad \quad \cancel{-7.4} \end{array}$$

$$\begin{array}{r} -1.9x = 13.4 \\ \cancel{-1.9} \quad \quad \quad \cancel{-1.9} \end{array}$$

$$\boxed{x = -7.05}$$

b) $2x - 4 = 2(x - 2)$

$$2x - 4 = 2x - 4$$

Infinitely Many Solutions

"IDENTITY"

d) $\frac{1}{2} = \frac{x-3}{x+1}$

$$1(x+1) = 2(x-3)$$

$$x+1 = 2x-6$$

$$\begin{array}{r} -x \quad \quad \quad -x \\ \hline 1 = x - 6 \end{array}$$

$$\begin{array}{r} +6 \quad \quad \quad +6 \\ \hline 7 = x \end{array}$$

$$\boxed{7 = x}$$

f) $|4x - 2| = 12$

$$\begin{array}{l} \swarrow \quad \searrow \\ 4x - 2 = 12 \quad \quad 4x - 2 = -12 \\ \begin{array}{r} \cancel{4x} - \cancel{2} = 12 \\ +2 \quad +2 \end{array} \quad \quad \begin{array}{r} \cancel{4x} - \cancel{2} = -12 \\ +2 \quad +2 \end{array} \end{array}$$

$$\begin{array}{r} 4x = 14 \\ \cancel{4} \quad \quad \quad \cancel{4} \end{array}$$

$$\boxed{x = \frac{7}{2}}$$

Reduce

$$\begin{array}{r} 4x = -10 \\ \cancel{4} \quad \quad \quad \cancel{4} \end{array}$$

$$\boxed{x = -\frac{5}{2}}$$

2) Solve each inequality and graph.

a) $2(x-4) \geq 6$

$$\begin{aligned} 2x - 8 &\geq 6 \\ +8 &+8 \\ \hline 2x &\geq 14 \\ \frac{2x}{2} &\geq \frac{14}{2} \\ \boxed{x} &\geq \boxed{7} \end{aligned}$$



b) $-\frac{m}{3} + 2 \leq 9$

$$\begin{aligned} -\frac{m}{3} + 2 &\leq 9 \\ -2 &-2 \\ \hline -\frac{m}{3} &\leq 7 \\ (-3) &(-3) \\ \hline \boxed{m} &\geq \boxed{-21} \end{aligned}$$



c) $2x + 10 \geq 7x + 7$

$$\begin{aligned} 2x + 10 &\geq 7x + 7 \\ -2x &-2x \\ \hline 10 &\geq 5x + 7 \\ -7 &-7 \\ \hline 3 &\geq 5x \\ \frac{3}{5} &\geq \frac{5x}{5} \\ \boxed{\frac{3}{5}} &\geq \boxed{x} \quad \text{or} \quad \boxed{x} \leq \boxed{\frac{3}{5}} \end{aligned}$$



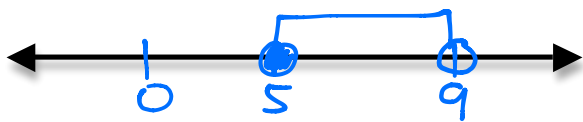
d) $2x - 10 > 3(-x + 5)$

$$\begin{aligned} 2x - 10 &> 3(-x + 5) \\ 2x - 10 &> -3x + 15 \\ +3x &+3x \\ \hline 5x - 10 &> 15 \\ +10 &+10 \\ \hline 5x &> 25 \\ \frac{5x}{5} &\frac{25}{5} \\ \boxed{x} &> \boxed{5} \end{aligned}$$



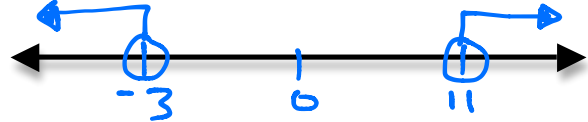
e) $7 \leq 3x - 8 < 19$

$$\begin{aligned} 7 \leq 3x - 8 < 19 \\ +8 &+8 \quad +8 \\ \hline 15 \leq 3x < 27 \\ \frac{15}{3} &\frac{3x}{3} < \frac{27}{3} \\ \boxed{5} &\leq \boxed{x} < \boxed{9} \end{aligned}$$



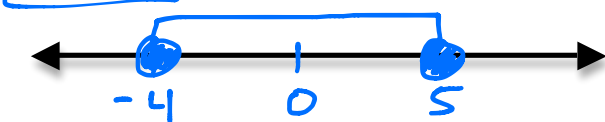
f) $-8x > 24$ or $2x - 5 > 17$

$$\begin{aligned} -8x &> 24 \\ \frac{-8x}{-8} &\frac{24}{-8} \\ \boxed{x} &< \boxed{-3} \\ 2x - 5 &> 17 \\ +5 &+5 \\ \hline 2x &> 22 \\ \frac{2x}{2} &\frac{22}{2} \\ \boxed{x} &> \boxed{11} \end{aligned}$$



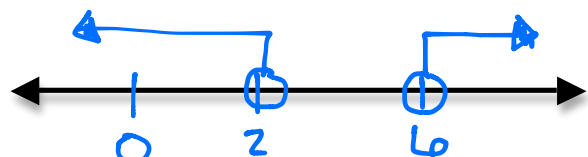
g) $|2x - 1| \leq 9$

$$\begin{aligned} 2x - 1 &\leq 9 & 2x - 1 &\geq -9 \\ +1 &+1 & +1 &+1 \\ \hline 2x &\leq 10 & 2x &\geq -8 \\ \frac{2x}{2} &\leq \frac{10}{2} & \frac{2x}{2} &\geq \frac{-8}{2} \\ \boxed{x} &\leq \boxed{5} & \boxed{x} &\geq \boxed{-4} \end{aligned}$$

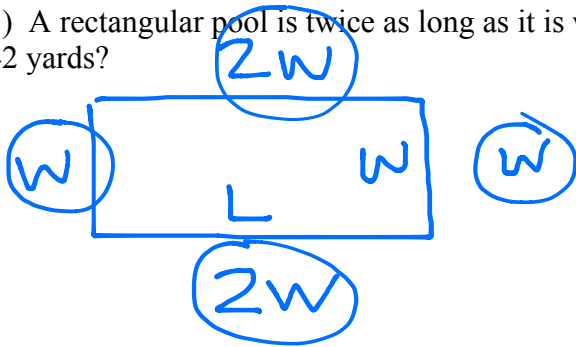


h) $|x - 4| > 2$

$$\begin{aligned} x - 4 &> 2 & x - 4 &< -2 \\ +4 &+4 & +4 &+4 \\ \hline \boxed{x} &> \boxed{6} & \boxed{x} &< \boxed{2} \end{aligned}$$



3) A rectangular pool is twice as long as it is wide. What are the dimensions of the pool if the perimeter is 42 yards?



$$P = 42 \text{ yds.}$$

$$L = 2w$$

$$w + 2w + w + 2w = 42$$

$$\frac{6w}{6} = \frac{42}{6}$$

$$\boxed{w = 7 \text{ yds.}} \\ \boxed{L = 14 \text{ yds.}}$$

4) A shopper's discount club charges a monthly fee of \$15 and sells gasoline for \$2.05 per gallon. The gas station across the street sells gasoline for \$2.35 per gallon and charges no fee. How many gallons of gasoline would you have to buy in one month to spend the same amount at either store?

$$15 + 2.05x = 2.35x$$

$$\frac{15}{.30} = \frac{.30x}{.30}$$

$$\boxed{50 \text{ gal.} = x}$$

If you buy 50 gallons of gas in one month, then the cost would be the same.

5) A DVD club charges a monthly membership fee of \$4.95 and \$11.95 for each DVD purchased. If Aaron's bill for the month was \$64.70, how many DVDs did Aaron purchase?

$$4.95 + 11.95x = 64.70$$

$$-4.95 \quad -4.95$$

$$\frac{11.95x}{11.95} = \frac{59.75}{11.95}$$

$$x = 5$$

$$\boxed{x = 5}$$

Aaron bought 5 DVD's

6) If it costs Mike \$11.79 in gasoline to drive 90 miles, how much will it cost him to drive 150 miles?

$$\frac{\$11.79}{90 \text{ miles}} = \frac{x}{150 \text{ miles}}$$

$$\frac{90x}{90} = \frac{1768.5}{90}$$

$$x = \$19.65$$

\$19.65 to drive 150 miles.

7) The sophomore class is putting on a variety show to raise money. It costs \$700 to rent the banquet hall they are going to use. If they charge \$15 for each ticket, how many tickets do they need to sell in order to raise at least \$1000?

$$\begin{array}{r} 15T - 700 > 1000 \\ + 700 \quad + 700 \\ \hline 15T > 1700 \\ \hline \frac{15T}{15} > \frac{1700}{15} \\ T > 113.33 \end{array}$$

They must sell at least 114 tickets.

$$\overline{T} \geq 114 \text{ tickets}$$

$$\& \ T > 113 \text{ tickets}$$

8) Write an inequality for each situation.

a) A car dealership sells at least 35 cars each week.

b) No more than 425 tickets to a musical will be sold.

$$x \geq 35$$

$$x \leq 425$$

9) Write a compound inequality for each situation.

a) A car salesman has been told to sell a particular car for more than \$14,500 and up to the sticker price of \$15,755.

b) The width of a parking space needs to be at least 8 feet and no more than 11 feet.

$$14500 < x \leq 15755$$

$$8 \leq x \leq 11$$