For question 1, find the exact unknown side length in simplified radical form. Does the triangle form a Pythagorean Triple?

1a. \[ x^2 = 16^2 + 10^2 \]
\[ 21^2 = x^2 + 10^2 \]
\[ 441 = x^2 + 100 \]
\[ \sqrt{341} = x \]
\[ x = \sqrt{341} \]
Is it a Pythagorean triple? **No**

1b. \[ x^2 = 20^2 + 16^2 \]
\[ x^2 = 400 + 256 \]
\[ x^2 = 656 \]
\[ x = \sqrt{656} \]
Is it a Pythagorean triple? **Yes**

2. Find the area of the shape below.

\[ \text{Area} = 15 \text{ m}^2 \]

3. a. You have a garden that is in the shape of a right triangle with one side that runs along a fence that measures 88 inches and another side that runs on the diagonal of the yard that measures 137 inches.
   b. What is the total perimeter of your garden?
   \[ 137^2 = 88^2 + x^2 \]
   \[ 18,769 = 7744 + x^2 \]
   \[ x^2 = 11,025 \]
   \[ x = 105 \text{ in} \]
   \[ \text{Perimeter} = 88 \text{ in} + 105 \text{ in} + 137 \text{ in} \]
   \[ = 330 \text{ in} \]
   
   b. Only one side of the garden is fenced. You plan to fence the rest of the garden to keep out the rabbits. You will need a fence post every 15 inches. If each post costs $1.25 and each foot of fencing costs $0.70, how much will it cost to enclose the garden?
   \[ \text{88 in is already fenced} \]
   \[ \text{So 105 in + 137 in = 242 in is left to fence} \]
   \[ \frac{242 \text{ in}}{15 \text{ in / post}} = 16.13 \text{ posts} \]
   \[ \text{We need 17 posts} \]
   \[ \frac{242 \text{ in}}{12 \text{ in/ft}} = 20.16 \text{ ft} \]
   \[ \text{We need 21 ft of fence} \]
   \[ 17 \text{ posts} \times (\$1.25 \text{ per post}) + 21 \text{ ft} \times (\$0.70 \text{ per foot}) \]
   \[ = 21.25 + 14.70 \]
   \[ = 35.95 \text{ dollars} \]
   
   c. What will be the square footage of your enclosed garden?
   \[ A = \frac{1}{2} bh = \frac{1}{2} (105 \text{ in}) (8 \text{ in}) = 420 \text{ in}^2 \]
   \[ = \frac{1.44}{12 \text{ in}} \]
   \[ \frac{1 \text{ ft}}{12 \text{ in}} = 32.083 \text{ ft}^2 \]

Multiple Choice

Let the numbers represent the lengths of the sides of a triangle. Which of the triangles are acute triangles?

- **A.** 3, 4, 5
- **B.** 6, 8, 10
- **C.** 7, 24, 26
- **D.** 9, 12, 15
- **E.** 8, 15, 17

Must have \( c^2 < a^2 + b^2 \)

So answer is **E.**

Multiple Choice

Which set of numbers can represent the side lengths of an obtuse triangle?

- **A.** 3, 4, 5
- **B.** 6, 8, 10
- **C.** 7, 24, 26
- **D.** 9, 12, 15
- **E.** 8, 15, 17

Must have \( c^2 > a^2 + b^2 \)

So answer is **D.**

4. You have a garden that is in the shape of a right triangle with one side that runs along a fence that measures 88 inches and another side that runs on the diagonal of the yard that measures 137 inches.

a. What is the total perimeter of your garden?

b. Only one side of the garden is fenced. You plan to fence the rest of the garden to keep out the rabbits. You will need a fence post every 15 inches. If each post costs $1.25 and each foot of fencing costs $0.70, how much will it cost to enclose the garden?

\[ \text{17 posts} \times (\$1.25 \text{ per post}) + 21 \text{ ft} \times (\$0.70 \text{ per foot}) \]
\[ = 21.25 + 14.70 \]
\[ = 35.95 \text{ dollars} \]

C. What will be the square footage of your enclosed garden?

\[ A = \frac{1}{2} bh = \frac{1}{2} (105 \text{ in}) (8 \text{ in}) = 420 \text{ in}^2 \]
\[ = \frac{1.44}{12 \text{ in}} \]
\[ \frac{1 \text{ ft}}{12 \text{ in}} = 32.083 \text{ ft}^2 \]
You want to build a square shed on an old concrete circular patio in your backyard. You want to maximize the amount of square footage in your shed by making sure your shed is square. Your friend told you to measure the diameter of the circular patio to find the dimensions of the square shed.

6a) Explain how this will help you find the length of the walls for your square shed.

6b) If you find the diameter of your circular patio is 22 feet, what will be the length of each wall?

7) Find the exact value of the indicated trig ratio given the triangle at the right as a fraction in simplified radical form.

a. \( \sin A = \frac{4}{7} \)

b. \( \cos B = \frac{4}{7} \)

c. \( \tan A = \frac{4}{\sqrt{33}} = \frac{4 \sqrt{33}}{33} \)

d. \( \sin B = \frac{\sqrt{33}}{7} \)

e. \( \cos A = \frac{\sqrt{33}}{7} \)

f. \( \tan B = \frac{\sqrt{33}}{4} \)

7a) Find the cosine of \( \angle B \).

7b) Find the sine of \( \angle A \).
8) Solve the right triangle. Round decimal answers to the nearest tenth

\[ \begin{align*}
\angle D &= 90^\circ - 31^\circ = 59^\circ \\
\tan(31^\circ) &= x/7.5 \\
x &= 17.5 \tan(31^\circ) \\
x &\approx 10.5 \\
\cos(31^\circ) &= y/17.5 \\
y &= 17.5 \cos(31^\circ) \\
y &\approx 17.5 \\
m \angle D &= 59^\circ
\end{align*} \]

\[ \begin{align*}
DF &= 20.4 \\
DE &= 10.5 \\
m \angle D &= 59^\circ
\end{align*} \]

9) \[ \begin{align*}
7.4^2 + 9.3^2 &= x^2 \\
54.76 + 86.49 &= x^2 \\
x &= \sqrt{141.25} \\
x &\approx 11.8841
\end{align*} \]

\[ \begin{align*}
\tan(R) &= 9.3/7.4 \\
R &= \tan^{-1}(9.3/7.4) \\
R &\approx 51.4908^\circ
\end{align*} \]

\[ \begin{align*}
RT &= 11.9 \\
m \angle T &= 38.5^\circ \\
m \angle R &= 51.5^\circ
\end{align*} \]

10) A wire cable is to be run from the top of a 600 ft tower to the ground. The horizontal distance from the base of the tower to the point where the cable is anchored is 100 ft. Draw a picture and label everything the problem has told you.

a. \[ \begin{align*}
\tan(x) &= \frac{600}{100} \\
x &= \tan^{-1} \left( \frac{600}{100} \right) \\
x &\approx 80.5^\circ
\end{align*} \]

Equation: \[ \frac{\tan x}{x} = \frac{600}{100} \]

b. Label the angle of elevation in the picture above as \( x^\circ \). What is the angle of elevation of the cable? (accurate to the nearest tenth of a degree) Write the equation you will use below.

Equation: \[ \tan x = \frac{600}{100} \]

angle of elevation = 80.5°

c. Cable is sold by the foot. Five extra feet of cable are required on each end of the cable to make the attachments. What is the length of the cable required to connect the cable to the tower?

\[ \begin{align*}
\tan(x) &= \frac{600}{100} \\
600 &= 608.2763 + 544 + 544 = 618.2763 \\
y &= 570,000 \\
608.2763 \\
y &= \sqrt{608.2763} \times 608.2763
\end{align*} \]

length of cable = 619 ft

11) A lighthouse keeper is standing on the edge of a cliff and looking at boat. The keeper measures the angle of depression as 5° and knows that the cliff is 60 feet tall.

a. Draw a picture and label everything the problem has told you.

b. How far away is the boat horizontally from the keeper? What is the line of sight distance from the keeper to the boat? Both answers should be accurate to the nearest tenth of a foot.

\[ \begin{align*}
\tan(5^\circ) &= \frac{60}{x} \\
x &= \frac{60}{\tan(5^\circ)} \approx 685.8 \\
\sin(5^\circ) &= \frac{60}{y} \\
y &= \frac{60}{\sin(5^\circ)} \approx 688.4
\end{align*} \]

Horizontal distance = 685.8 ft

Line of sight distance = 688.4 ft