

Chapter 10

Simple Harmonic Motion

Simple Harmonic Motion

- Vibration about an equilibrium position in which a restoring force is proportional to the displacement from equilibrium

Equilibrium Position

$F_{elastic} = 0$
 $x = 0$

- Position where net force is equal to zero
- Natural resting place
- Velocity is at maximum
- Acceleration is zero

Restoring Force

- Force that causes simple harmonic motion
- Proportional to the displacement
- Maximum displacement
 - Acceleration is maximum
 - Velocity is zero

$$F_{elastic} = -kx$$

Simple Pendulum

- Restoring force is the bob's weight
- Weight is broken into perpendicular components
- The net force is the gravitational force in the x-direction

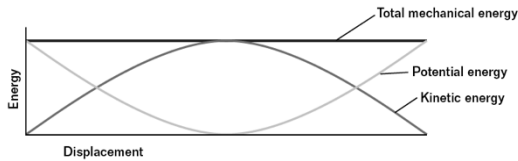
Simple Harmonic Motion

Maximum displacement			$F_x = F_{max}$ $a = a_{max}$ $v = 0$
Equilibrium			$F_x = 0$ $a = 0$ $v = v_{max}$
Maximum displacement			$F_x = F_{max}$ $a = a_{max}$ $v = 0$
Equilibrium			$F_x = 0$ $a = 0$ $v = v_{max}$
Maximum displacement			$F_x = F_{max}$ $a = a_{max}$ $v = 0$

$-A \quad 0 \quad A \quad x$

Energy Changes in SHM

- Potential energy is proportional to displacement
- Kinetic energy is inversely proportional to displacement



Amplitude, Period, and Frequency

- Amplitude - Maximum displacement from equilibrium
 - Radians or meters
- Period - Time it takes to execute a complete motion
 - Seconds
- Frequency - Number of cycles or vibrations per unit of time
 - Hertz

Period of Pendulum

- Depends on
 - Length
 - Acceleration of gravity

$$T = 2\pi\sqrt{\frac{L}{g}}$$

Period of Mass-Spring System

- Depends on
 - Mass
 - Spring constant

$$T = 2\pi\sqrt{\frac{m}{k}}$$

Elastic Deformation

- Stretching and Compression

$$F = Y\left(\frac{\Delta L}{L_0}\right)A$$

- Y=Young's Modulus
 - Different for each solid
 - N/m²
 - p. 291

Elastic Deformation

- Shear deformation

$$F = S\left(\frac{\Delta X}{L_0}\right)A$$

- S=Shear Modulus
 - Different for each solid
 - N/m²
 - p. 291

Elastic Deformation

- Volume deformation

$$\Delta P = -B \left(\frac{\Delta V}{V_0} \right)$$

- B=Bulk Modulus
 - Different for each solid and liquid
 - N/m²
 - p. 293

Stress and Strain

- **Stress** is proportional to **Strain**

$$\frac{F}{A} = Y \left(\frac{\Delta L}{L_0} \right)$$

$$\frac{F}{A} = S \left(\frac{\Delta X}{L_0} \right)$$

$$\Delta P = B \left(-\frac{\Delta V}{V_0} \right)$$